## Section 1.3 Guided Notebook

## Section 1.3 Complex Numbers

$\square \quad$ Work through Section 1.3 TTK
$\square \quad$ Work through Objective 1
$\square \quad$ Work through Objective 2
Work through Objective 3
Work through Objective 4
Work through Objective 5

## Section 1.3 Complex Numbers

### 1.3 Things To Know

1. Simplifying Radical Expressions Using the Product Rule

Can you simply the radical expression $\sqrt{12}$ or $\sqrt{50 x^{4} y^{3}}$ ? Work through the animation and video and then try working through a "You Try It" problem or refer to Section R.3.

## THE IMAGINARY UNIT

Take notes on the video that explains the imaginary unit here:

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What is the definition of the imaginary unit?

Section 1.3 Objective 1 Simplifying Powers of $i$

Explain the cyclic nature of powers of $i$ :

Work through Example 1 and take notes here:
Simplify each of the following:
a. $i^{43}$
b. $i^{100}$
c. $i^{-21}$

## COMPLEX NUMBERS

What is a complex number?

Give several examples of complex numbers.

Is every real number considered a complex number? Why or why not?

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## Section 1.3 Objective 2 Adding and Subtracting Complex Numbers

Watch the video, work through Example 2 and explain how to add/subtract complex numbers.

Perform the indicated operations:
a. $(7-5 i)+(-2-i)$
b. $(7-5 i)-(-2-i)$

## Section 1.3 Objective 3 Multiplying Complex Numbers

Fill in the blanks:
When multiplying complex numbers, treat the problem as if it were the multiplication of two
$\qquad$ . Just remember that $\qquad$ $=$ $\qquad$ .

Work through Example 3 and show your work here. Watch the video to check your solution.

Multiply (4-3i)(7+5i).

Example 4: Simplify $(\sqrt{3}-5 i)^{2}$. Work through the video that accompanies Example 4 and write your notes here:

What is the definition of a complex conjugate?

Work through Example 5 and show your work:
Multiply the complex number $z=-2-7 i$ by its complex conjugate $\bar{z}=-2+7 i$.

What will always happen when you multiply a complex number by its complex conjugate?

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## Section 1.3 Objective 4 Finding the Quotient of Complex Numbers

What is the goal when dividing two complex numbers?

Work through Example 6 and take notes here. Watch the video at the top of page 1.3-11 to check your solution.
Write the quotient in the form $a+b i: \frac{1-3 i}{5-2 i}$

## Section 1.3 Objective 5 Simplifying Radicals with Negative Radicands

Write down the property seen on page 1.3-12.

Work through Example 7 and write your notes here: Simplify: $\sqrt{-108}$

True or False: $\sqrt{a} \sqrt{b}=\sqrt{a b}$ for all real numbers $a$ and $b$. Explain.

Work through Example 8 and write your notes here: Simplify the following expressions:
a) $\sqrt{-8}+\sqrt{-18}$
b) $\sqrt{-8} \cdot \sqrt{-18}$
c) $\frac{-6+\sqrt{(-6)^{2}-4(2)(5)}}{2}$
d) $\frac{4 \pm \sqrt{-12}}{4}$

