

6.5 Practice Problems

In problems 1 - 4, use the properties of logarithms to expand each logarithmic expression as much possible. Where possible, evaluate logarithmic expressions without using a calculator.

$$1. \log(10000xy)$$

$$\begin{aligned} &= \log 10000 + \log x + \log y \\ &= 4 + \log x + \log y \end{aligned}$$

$$2. \log_3\left(\frac{81}{x}\right)$$

$$\begin{aligned} &= \log_3 81 - \log_3 x \\ &= 4 - \log_3 x \end{aligned}$$

$$3. \ln\left(\frac{e^3}{x}\right)$$

$$\begin{aligned} &= \ln e^3 - \ln x \\ &= 3 \ln e - \ln x \end{aligned}$$

$$4. \log_4\left(\frac{16x^2}{y^3}\right)$$

$$\begin{aligned} &= \log_4 16 + \log_4 x^2 - \log_4 y^3 \\ &= 2 + 2 \log_4 x - 3 \log_4 y \end{aligned}$$

In problems 5 - 8, use properties of logarithms to condense each logarithmic expression. Write the expression as a single logarithm whose coefficient is 1.

$$5. \log 25 + \log 4$$

$$\begin{aligned} &= \log(25)(4) \\ &= \log 100 \\ &= 2 \end{aligned}$$

$$6. \log_2 x - \log_2 y$$

$$= \log_2\left(\frac{x}{y}\right)$$

$$7. 2 \ln x + 4 \ln y - 3 \ln z$$

$$\begin{aligned} &= \ln x^2 + \ln y^4 - \ln z^3 \\ &= \ln\left(\frac{x^2 y^4}{z^3}\right) \end{aligned}$$

$$8. 2 \log_3 x - 3 \log_3 y$$

$$\begin{aligned} &= \log_3 x^2 - \log_3 y^3 \\ &= \log_3\left(\frac{x^2}{y^3}\right) \end{aligned}$$

In problems 9 - 10, use common logarithms or natural logarithms and a calculator to evaluate to four decimal places. (Use the change of base formula.)

$$9. \log_8 25 = \frac{\log 25}{\log 8} = \frac{\ln 25}{\ln 8} \approx 1.548 \quad 10. \log_{27} 13 = \frac{\log 13}{\log 27} = \frac{\ln 13}{\ln 27} \approx .7182$$

In problems 11 - 12, simplify using properties of logarithms.

$$11. 2^{\log_2(2x-9)}$$

$$= 2x-9$$

$$12. \log_9 9^{1-8x}$$

$$= 1-8x$$

If $f(x) = \ln x$, $g(x) = e^{8x}$, and $h(x) = x^6$, find the following.

$$a. (f \circ g)(x)$$

$$b. \text{ domain of } (f \circ g)(x)$$

$$c. (f \circ g)(3)$$

$$= \ln e^{8x} = 8x$$

$$(-\infty, \infty)$$

$$g(3) = 24$$

$$d. (g \circ f)(x)$$

$$e^{8(\ln x)} = x^6$$

$$e. \text{ domain of } (g \circ f)(x)$$

$$(0, \infty)$$

$$f. (f \circ h)(x)$$

$$\ln x^6$$

$$g. \text{ domain of } (f \circ h)(x)$$

$$(-\infty, 0) \cup (0, \infty)$$

$$h. (f \circ h)(e)$$

$$\begin{aligned} \ln e^6 &= 6 \ln e \\ &= 6(1) \\ &= 6 \end{aligned}$$