

3.1 Practice Problems

1. Find the domain and range given the set of points. $\{(2,4), (4,-2), (5,8), (-4,7), (7,-8)\}$

$$\text{domain} = \{2, 4, 5, -4, 7\}$$

$$\text{range} = \{4, -2, 8, 7, -8\}$$

2. Determine if the relation given in #1 is a function.

yes

3. Determine if the following equations represent functions.

a. $y = x^2 + 4$

yes

b. $y = |x + 4|$

yes

c. $x^2 + y^2 = 16$

$$-x^2 \quad -x^2$$

$$y^2 = 16 - x^2$$

$$\sqrt{y^2} = \sqrt{16 - x^2}$$

$$y = \pm \sqrt{16 - x^2}$$

no

4. Let $f(x) = x^2 + 3x - 5$ and find the following.

a. $f(5)$

$$\begin{aligned} f(5) &= 5^2 + 3(5) - 5 \\ &= 25 + 15 - 5 \\ &= 40 - 5 \\ &= 35 \end{aligned}$$

b. $f(-2)$

$$\begin{aligned} f(-2) &= (-2)^2 + 3(-2) - 5 \\ &= 4 - 6 - 5 \\ &= -2 - 5 \\ &= -7 \end{aligned}$$

c. $f(a+5)$

$$\begin{aligned} f(a+5) &= (a+5)^2 + 3(a+5) - 5 \\ &= a^2 + 10a + 25 + 3a + 15 - 5 \\ &= a^2 + 13a + 20 \end{aligned}$$

d. $f(-x)$

$$\begin{aligned} f(-x) &= (-x)^2 + 3(-x) - 5 \\ &= x^2 - 3x - 5 \end{aligned}$$

e) $\frac{f(x+h) - f(x)}{h}$

$$= \frac{(x+h)^2 + 3(x+h) - 5 - (x^2 + 3x - 5)}{h}$$

$$= \frac{x^2 + 2xh + h^2 + 3x + 3h - 5 - x^2 - 3x + 5}{h}$$

$$= \frac{2xh + h^2 + 3h}{h} = 2x + h + 3$$

5. Find the domain of the following functions.

a. $f(x) = 2x^2 - 3x + 9$

All real numbers
or
 $(-\infty, \infty)$

b. $g(x) = \frac{2x+3}{x-2}$

$\{x \mid x \neq 2\}$
or
 $(-\infty, 2) \cup (2, \infty)$

c. $h(x) = \sqrt{x+5}$

$\{x \mid x \geq -5\}$
or
 $[-5, \infty)$

d. $g(x) = \frac{\sqrt{x+1}}{x-9}$

$\{x \mid x \geq -1 \text{ and } x \neq 9\}$
or
 $[-1, 9) \cup (9, \infty)$

e. $h(x) = \frac{3}{x^2 - 3x - 4}$

$\{x \mid x \neq 4 \text{ and } x \neq -1\}$
or
 $(-\infty, -1) \cup (-1, 4) \cup (4, \infty)$

f. $f(x) = \sqrt{2-3x}$

$\{x \mid x \leq \frac{2}{3}\}$
or
 $(-\infty, \frac{2}{3}]$

6. Find $f+g$, $f-g$, fg , and $\frac{f}{g}$ if $f(x) = x^2 - 25$ and $g(x) = x^2 + 2x - 15$.

Determine the domain for each function.

$D_f = (-\infty, \infty)$ $D_g = (-\infty, \infty)$

$$(f+g)(x) = f(x) + g(x) = x^2 - 25 + x^2 + 2x - 15 = 2x^2 + 2x - 35$$

$$D_{f+g} = (-\infty, \infty)$$

$$(f-g)(x) = f(x) - g(x) = x^2 - 25 - (x^2 + 2x - 15) = x^2 - 25 - x^2 - 2x + 15 = -2x - 10$$

$$D_{f-g} = (-\infty, \infty)$$

$$(fg)(x) = f(x)g(x) = (x^2 - 25)(x^2 + 2x - 15) = x^4 + 2x^3 - 15x^2 - 25x^2 - 50x + 375 = x^4 + 2x^3 - 40x^2 - 50x + 375$$

$$D_{fg} = (-\infty, \infty)$$

$$\left(\frac{f}{g}\right)(x) = \frac{f(x)}{g(x)} = \frac{x^2 - 25}{x^2 + 2x - 15} = \frac{(x+5)(x-5)}{(x+5)(x-3)} = \frac{x-5}{x-3}$$

$$D_{\frac{f}{g}} = (-\infty, -5) \cup (-5, 3) \cup (3, \infty)$$