

MAC1105 College Algebra
4.2 Practice Problems

1. You have 80 yards of fencing to enclose a rectangular region. Find the dimensions of the rectangle that maximize the enclosed area. What is the maximum area?

2. A person standing close to the edge on the top of a 96 foot building throws a baseball vertically upward. The quadratic function

$$s(t) = -16t^2 + 16t + 96$$

models the ball's height above the ground, $s(t)$, in feet, t seconds after it was thrown.

- After how many seconds does the ball reach its maximum height? What is the maximum height?
- How many seconds does it take until the ball finally hits the ground?
- Find $s(0)$ and describe what this means.

3. The monthly revenue R achieved by selling x baseball gloves is figured to be $R(x) = 80x - 0.5x^2$. The monthly cost C of selling x baseball gloves is $C(x) = 20x + 1000$.

- How many baseball gloves must the company sell to maximize revenue? What is the maximum revenue? (Round to the nearest integer as needed)
- Profit is given as $P(x) = R(x) - C(x)$. What is the profit function?
- How many baseball gloves must the company sell to maximize profit? What is the maximum profit?

4. The marketing department at a electronics company has found that, when certain tablets are sold at a price of p dollars per unit, the number x of tablets sold is given by the demand equation

$$x = 35000 - 100p$$

- a. Find a model that expresses the revenue R as a function of the price p .
- b. What is the domain of R ?
- c. What unit price should be used to maximize revenue?
- d. If this price is charged, what is the maximum revenue?
- e. How many units are sold at this price?

5. A projectile is fired from a cliff 180 feet above the water at an inclination of 45° to the horizontal, with a muzzle velocity of 45 feet per second. The height h of the projectile above the water is given by

$$h(x) = \frac{-32x^2}{(45)^2} + x + 180$$

where x is the horizontal distance of the projectile from the face of the cliff. Use this information to answer the following.

- a. At what horizontal distance from the face of the cliff is the height of the projectile a maximum.
- b. Find the maximum height of the projectile.